

# Topics in Algebra, Trigonometry and Pre-Calculus

21st February 2010

## Round-up Homework.

### Instructions

Please note that the following questions relate to the following units:

- Q1 and Q2: Systems of inequalities.
- Q3 and Q4: Logarithms and Exponential functions.
- Q5 and Q6: Applications of Logarithms and Exponential functions.

1. Sketch the following region in the  $xy$ -plane:  $\{(x, y) \mid |x| < 2 \text{ and } |y| \geq 3\}$ .
2. Sketch the following region in the  $xy$ -plane:  $\{(x, y) \mid -2 \leq y \leq x + 2 \text{ and } y < 5 - x\}$ .
3. Use all the properties of logarithms to evaluate (i.e. make it into a single expression) the following:

$$\log_2(6) - \log_2(15) + \log_2(20).$$

4. Find  $x$  such that  $2^{5x-2} = 15^{x+1}$ .
5. If I invest \$1000 for 12 years at a compound interest rate of 15% then how much will my investment be worth?
6. A bottle of pop has temperature  $T(t)$  (in Farenhiet) given by the following formula:

$$T(t) = 44 + 28e^{-0.01663t}$$

, where  $t$  is the number of minutes the pop has been cooling. How long does it take for the bottle to reach  $50^\circ F$ ?